

There may be a time where you need to multiple both equations by a different number to eliminate a variable.

Example 1: $\begin{cases} -5x + 2y = 32 & \cdot 2 \\ 2x + 3y = 10 & \cdot 5 \end{cases}$

$$\begin{array}{r} -10x + 4y = 64 \\ 10x + 15y = 50 \\ \hline \end{array}$$

$$\begin{array}{r} 19y = 114 \\ 19 \quad 19 \end{array}$$

$$\boxed{y = 6}$$

$$2x + 3y = 10$$

$$2x + 3(6) = 10$$

$$2x + 18 = 10$$

$$\begin{array}{r} -18 \quad -18 \\ \hline \end{array}$$

$$\begin{array}{r} 2x = -8 \\ 2 \quad 2 \end{array}$$

$$\boxed{x = -4}$$

$$\boxed{(-4, 6)}$$

Example 2: $\begin{cases} 2x + 5y = 26 & \cdot 3 \\ -3x - 4y = -25 & \cdot 2 \end{cases}$

$$\begin{array}{r} 6x + 15y = 78 \\ -6x - 8y = -50 \\ \hline \end{array}$$

$$\begin{array}{r} 7y = 28 \\ 7 \quad 7 \end{array}$$

$$\boxed{y = 4}$$

$$2x + 5y = 26$$

$$2x + 5(4) = 26$$

$$\begin{array}{r} 2x + 20 = 26 \\ -20 \quad -20 \\ \hline \end{array}$$

$$\begin{array}{r} 2x = 6 \\ 2 \quad 2 \end{array}$$

$$\boxed{x = 3}$$

$$\boxed{(3, 4)}$$

There may be a time where you need to rearrange one or both of the equations so they are in standard form ($Ax + By = C$). You always want the variables to line up so you can use the elimination process.

Example 3:
 $2x + y = 25$
 $3y = 2x - 13$

$$\begin{array}{r} -2x \quad -2x \\ \hline -2x + 3y = -13 \\ 2x + y = 25 \\ \hline 4y = 12 \\ \frac{4y}{4} = \frac{12}{4} \\ \boxed{y = 3} \end{array}$$

$$2x + y = 25$$

$$\begin{array}{r} 2x + 3y = 25 \\ -3 \quad -3 \\ \hline \end{array}$$

$$\frac{2x}{2} = \frac{22}{2}$$

$$\boxed{x = 11}$$

$$\boxed{(3, 11)}$$

Example 4:
 $-3x + 4y = -18$
 $x = -2y - 4$

$$\begin{array}{r} +2y \quad +2y \\ \hline 3(x + 2y = -4) \\ -3x + 4y = -18 \\ \hline 3x + 6y = -12 \\ \hline 10y = -30 \\ \frac{10y}{10} = \frac{-30}{10} \\ \boxed{y = -3} \end{array}$$

$$x = -2y - 4$$

$$x = -2(-3) - 4$$

$$x = 6 - 4$$

$$\boxed{x = 2}$$

$$\boxed{(2, -3)}$$

Example 5:
 $3(-2x + 3y = -15)$
 $2(3x + 2y = -23)$

$$\begin{array}{r} -6x + 9y = -45 \\ 6x + 4y = -46 \\ \hline 13y = -91 \\ \frac{13y}{13} = \frac{-91}{13} \\ \boxed{y = -7} \end{array}$$

$$-2x + 3y = -15$$

$$-2x + 3(-7) = -15$$

$$-2x - 21 = -15$$

$$\frac{-2x}{-2} = \frac{6}{-2}$$

$$\frac{-2x}{-2} = \frac{6}{-2}$$

$$\boxed{x = -3}$$