

7.5 Notes

Factoring Special Products

Perfect Square Trinomials:

1.) $x^2 + 12x + 36$

$$x^2 + 6x + 6x + 36$$

$$\begin{array}{r} 36 \\ \hline 6 \quad 6 \\ \hline 12 \end{array}$$

$$x(x+6) + 6(x+6)$$

$$\boxed{\begin{array}{l} (x+6)(x+6) \\ \text{or} \\ (x+6)^2 \end{array}}$$

2.) $x^2 + 8x + 16$

$$x^2 + 4x + 4x + 16$$

$$\begin{array}{r} 16 \\ \hline 4 \quad 4 \\ \hline 8 \end{array}$$

$$x(x+4) + 4(x+4)$$

$$\boxed{\begin{array}{l} (x+4)(x+4) \\ \text{or} \\ (x+4)^2 \end{array}}$$

3.) $4x^2 - 12x + 9$

$$4x^2 - 6x + 6x + 9$$

$$\begin{array}{r} 36 \\ \hline -6 \quad -6 \\ \hline -12 \end{array}$$

$$2x(2x-3) - 3(2x-3)$$

$$\boxed{\begin{array}{l} (2x-3)(2x-3) \\ \text{or} \\ (2x-3)^2 \end{array}}$$

4.) $9x^2 - 12x + 4$

$$9x^2 - 6x + 6x + 4$$

$$\begin{array}{r} 36 \\ \hline -6 \quad -6 \\ \hline -12 \end{array}$$

$$3x(3x-2) - 2(3x-2)$$

$$\boxed{\begin{array}{l} (3x-2)(3x-2) \\ \text{or} \\ (3x-2)^2 \end{array}}$$

5.) $x^2 + 6x + 9$

$$x^2 + 3x + 3x + 9$$

$$\begin{array}{r} 9 \\ \hline 3 \quad 3 \\ \hline 6 \end{array}$$

$$x(x+3) + 3(x+3)$$

$$\boxed{\begin{array}{l} (x+3)(x+3) \\ \text{or} \\ (x+3)^2 \end{array}}$$

6.) $4x^2 + 20x + 25$

$$4x^2 + 10x + 10x + 25$$

$$\begin{array}{r} 100 \\ \hline 10 \quad 10 \\ \hline 20 \end{array}$$

$$2x(2x+5) + 5(2x+5)$$

$$\boxed{\begin{array}{l} (2x+5)(2x+5) \\ \text{or} \\ (2x+5)^2 \end{array}}$$

Try it!

7.) $x^2 + 14x + 49$

$$(x+7)^2$$

8.) $4x^2 - 4x + 1$

$$(2x-1)^2$$

perfect squares

1, 4, 9, 16, 25, 36, 49, 64, 81, 100...

Difference of two squares:

$$a^2 - b^2$$

$$(\underline{a} + \underline{b})(\underline{a} - \underline{b})$$

what squared gives you each term?

1.) $x^2 - \frac{4}{2}$

$$(x+2)(x-2)$$

2.) $x^2 - \frac{16}{4}$

$$(x+4)(x-4)$$

3.) $49 - p^2$
7 p *don't flip the order!*

$$(7+p)(7-p)$$

4.) $25m^2 - 81$
5m 9

$$(5m+9)(5m-9)$$

5.) $16n^2 - 9$
4n 3

$$(4n+3)(4n-3)$$

6.) $x^4 - 49$
 x^2 7

$$(x^2+7)(x^2-7)$$

* $x^6 - 49$ $x^8 - 49$
 $(x^3+7)(x^3-7)$ $(x^4+7)(x^4-7)$
*with a variable, you divide the exponent in half.

Try it!

7.) $n^2 - 25$

$$(n+5)(n-5)$$

8.) $4m^2 - 25$

$$(2m+5)(2m-5)$$

9.) $k^4 - 36$

$$(k^2+6)(k^2-6)$$

10.) $9n^2 - 1$

$$(3n+1)(3n-1)$$

*this only works with subtraction $\rightarrow x^2 + 16$ is "not factorable"

Factor completely. **Note** You may need to factor the GCF first.

1.) $2x^2 - 18$

$$2(x^2 - 9)$$
$$2(x+3)(x-3)$$

2.) $4a^2 - 100$

$$4(a^2 - 25)$$
$$4(a+5)(a-5)$$

3.) $32 - 2y^2$

$$2(16 - y^2)$$
$$2(4+y)(4-y)$$

Try it!

4.) $9x^2 - 36y^2$

$$9(x^2 - 4y^2)$$
$$9(x+2y)(x-2y)$$

5.) $25a^2 + 100$

$$25(a^2 + 4)$$

can't factor
any further

6.) $27x^3 - 3x$

$$3x(9x^2 - 1)$$
$$3x(3x+1)(3x-1)$$

